

Chapter 2 Equations in One Variable

Lesson 2-5 Solve Multi-Step Equations

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3 Solve $\frac{1}{3}h - 4\left(\frac{2}{3}h - 3\right) = \frac{2}{3}h - 6$. Check your solution.

$$\begin{aligned}\frac{1}{3}h - 4\left(\frac{2}{3}h - 3\right) &= \frac{2}{3}h - 6 && \text{Write the equation.} \\ \frac{1}{3}h - \frac{8}{3}h + 12 &= \frac{2}{3}h - 6 && \text{Distributive Property} \\ -\frac{7}{3}h + 12 &= \frac{2}{3}h - 6 && \text{Collect like terms.} \\ +\frac{7}{3}h &= +\frac{7}{3}h && \text{Addition Property of Equality} \\ \hline 12 &= 3h - 6 && \text{Simplify.} \\ +6 &= \quad +6 && \text{Addition Property of Equality} \\ 18 &= 3h && \text{Simplify.} \\ \frac{18}{3} &= \frac{3h}{3} && \text{Division Property of Equality} \\ 6 &= h && \text{Simplify.}\end{aligned}$$

So, the solution is 6.

To check the solution, replace h with 6 in the original equation.

$$\begin{aligned}\frac{1}{3}h - 4\left(\frac{2}{3}h - 3\right) &= \frac{2}{3}h - 6 && \text{Write the original equation.} \\ \frac{1}{3}[6] - 4\left(\frac{2}{3}[6] - 3\right) &\stackrel{?}{=} \frac{2}{3}[6] - 6 && \text{Replace } h \text{ with 6.} \\ 2 - 4(4 - 3) &\stackrel{?}{=} 4 - 6 && \text{Simplify.} \\ 2 - 4(1) &\stackrel{?}{=} -2 && \text{Simplify.} \\ 2 - 4 &\stackrel{?}{=} -2 && \text{Simplify.} \\ -2 &= -2 \checkmark && \text{The sentence is true.}\end{aligned}$$



The school has budgeted \$2,000 for an end-of-year party at the local park. The cost to rent the park shelter is \$150. How much can the student council spend per student on food if each of the 225 students received a \$3.50 gift?

Let f represent the amount spent per student on food. Then $f + 3.50$ represents the total amount spent per student. There are 225 students and the park shelter costs \$150.

$$225(f + 3.5) + 150 = 2,000$$

Write the equation.

$$225f + 225 \cdot 3.5 + 150 = 2,000$$

Distributive Property

$$225f + 787.5 + 150 = 2,000$$

Simplify.

$$225f + 937.5 = 2,000$$

Simplify.

$$225f + 937.5 - 937.5 = 2,000 - 937.5$$

Subtraction Property of Equality

$$225f = 1,062.5$$

Simplify.

$$\frac{225f}{225} = \frac{1,062.5}{225}$$

Division Property of Equality

$$f = 4.\overline{72}$$

Simplify.

So, the student council can spend \$4.72 per student on food.